

# Turkish Journal of Electrical Engineering & Computer Sciences

http://journals.tubitak.gov.tr/elektrik/

Research Article

Turk J Elec Eng & Comp Sci (2015) 23: 2138 – 2149 © TÜBİTAK doi:10.3906/elk-1301-183

# Grounded capacitor-based new floating inductor simulators and a stability test

## Erkan YUCE<sup>1</sup>, Sezai TOKAT<sup>2,\*</sup>, Halil ALPASLAN<sup>1</sup>

<sup>1</sup>Department of Electrical and Electronics Engineering, Faculty of Engineering, Pamukkale University, Denizli, Turkey

Received: 24.01.2013 • Accepted/Published Online: 14.08.2013 • Printed: 31.12.2015

**Abstract:** In this paper, two new floating inductor simulators (FISs), both using two differential difference current conveyors, are considered. The proposed FISs do not suffer from passive component matching constraints and employ a minimum number of passive elements. They use a grounded capacitor; accordingly, they are suitable for integrated circuit technology. They have good low- and high-frequency performances. Simulations are performed with the SPICE program to verify the claimed theory. Moreover, for the first FIS used in a second-order low-pass filter, a stability test is performed as an example.

Key words: Floating inductor simulator, differential difference current conveyor, stability test

#### 1. Introduction

The use of current-mode active devices has some potential advantages over their voltage-mode counterparts such as operational amplifiers (OAs) [1]. These advantages are wider bandwidth, higher linearity, greater dynamic range, freedom from slew-rate limitations, freedom from trade-off between speed and bandwidth, usage of less number of active devices, etc. [1].

Floating inductor simulators (FISs) [2–28] are basic building blocks for analog signal processing systems because implementing spiral inductors in integrated circuit (IC) technology is still difficult due to some of their drawbacks, such as large silicon area, high cost, lack of electronic tunability, and low quality factor. A single active device is used in [2–4], whereas their internal structures are complex. The devices in [3–16] are made up of only grounded passive components, but only [14] has the property of improved low-frequency performance. Furthermore, [2], [17], [20], [24], and [26] do not have the property of improved low-frequency performances. The devices in [10] and [16–18] require critical passive component matching condition(s). The ones in [18], [19], and [25] use a floating capacitor, while [18] and [23] employ two capacitors. The devices in [14] and [21–23] cannot be operated at higher frequencies because they have capacitor(s) connected in series to the X terminal of the active device(s). The devices in [9–12], [15–17], [21], [23], and [24] are composed of more than two active devices. Finally, the devices in [25] and [28] consist of OAs and [5] and [6] include operational transconductance amplifiers, which have limited high-frequency performances.

A differential difference current conveyor (DDCC) has the advantages of a second-generation current conveyor and a differential difference amplifier, which possesses high input impedances and arithmetic operation

<sup>&</sup>lt;sup>2</sup>Department of Computer Engineering, Faculty of Engineering, Pamukkale University, Denizli, Turkey

<sup>\*</sup>Correspondence: stokat@pau.edu.tr

capability [29]. On the other hand, a grounded capacitor, when compared to a floating one, is simpler to implement in IC fabrication. Furthermore, the floating capacitor has substantial parasitic capacitances [30].

In this study, two new FIS circuits are proposed. Both FISs have the properties of improved low-frequency performances because they do not suffer from Z terminal parasitic resistors [27]. Both are composed of two DDCCs as active components and a minimum number of passive components. Both proposed FIS circuits are devoid of component matching constraints and use a grounded capacitor, which makes them suitable for IC process [31]. Electronically tunable FISs can be easily obtained by replacing only the current-controlled DDCC [32] instead of both DDCCs of the proposed FISs and removing both resistors. Computer simulation results using the SPICE program are compared with ideal ones for confirmation. Furthermore, a stability test for the first FIS used in a second-order low-pass filter example is performed as an example.

## 2. Suggested circuits

Using standard notation, a six-terminal DDCC whose electrical symbol is shown in Figure 1 can be characterized by the following matrix equation:

where k = 1, 2 denotes the kth active device. In Figure 1,  $\alpha$  and  $\gamma$  are frequency-dependent nonideal current gains and  $\beta$  is frequency-dependent nonideal voltage gain, which are all ideally equal to unity.

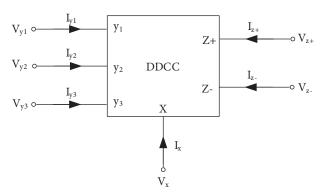


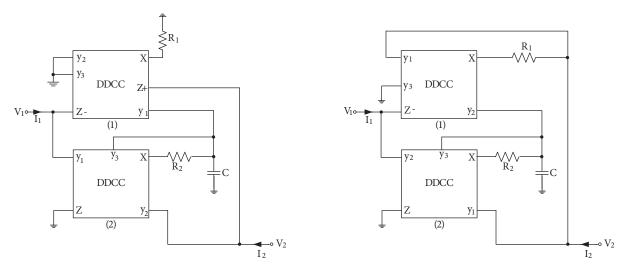
Figure 1. Electrical symbol of the six-terminal DDCC.

Applying straightforward analysis to the FIS topologies in Figures 2 and 3, the following matrix equation is ideally found to be:

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \frac{1}{sCR_1R_2} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}. \tag{2}$$

Note that the FIS topologies in Figures 2 and 3 have only resistors but no capacitors connected in series to the X terminals of the DDCCs; thus, they can be operated at higher frequencies [33], which is one of the most important properties of the proposed FISs. The high-frequency performance of both of the proposed FISs can

be further increased by the method given in [34]. Ideal and nonideal representations of an FIS are respectively given in Figures 4a and 4b. In Figure 5, representation of the first proposed FIS for the stability test is given.



**Figure 2.** The first proposed floating inductor simulator circuit.

**Figure 3.** The second proposed floating inductor simulator circuit.

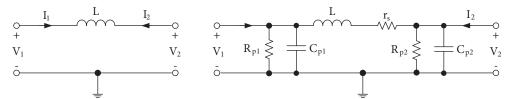


Figure 4. Representation of the FISs given in Figures 2 and 3: a) ideal, b) nonideal.

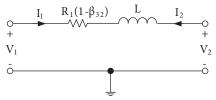


Figure 5. Floating inductor simulator representation of Figure 2 for stability test.

If nonideal gains are considered, the first proposed FIS in Figure 2 can be expressed by the following matrix equation:

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \frac{\beta_{11}}{sCR_1R_2 + R_1(1 - \beta_{32})} \begin{bmatrix} \beta_{12}\gamma_1 & -\beta_{22}\gamma_1 \\ -\alpha_1\beta_{12} & \alpha_1\beta_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}.$$
 (3)

For simplicity, it is assumed that all the nonideal gains except  $\beta_{11}$  and  $\beta_{32}$  are equal to unity. Then matrix equation in Eq. (3) turns into

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \frac{\beta_{11}}{sCR_1R_2 + R_1(1 - \beta_{32})} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$

$$= \frac{1}{sL_{eq} + R_{eq}} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$

$$(4)$$

Here,  $L_{eq} = CR_1R_2/\beta_{11}$  and  $R_{eq} = R_1(1-\beta_{32})/\beta_{11}$ . Therefore, active and passive sensitivities are calculated as:

$$\begin{split} S_C^{L_{eq}} &= S_{R_1}^{L_{eq}} = S_{R_2}^{L_{eq}} = -S_{\beta_{11}}^{L_{eq}} = 1 \\ S_{R_1}^{R_{eq}} &= -S_{\beta_{11}}^{R_{eq}} = 1 \\ S_{\beta_{32}}^{R_{eq}} &= \frac{\beta_{32}}{\beta_{32} - 1} \end{split} \tag{5}$$

The FIS in Figure 3 can be expressed as:

$$I_{1} = \frac{\beta_{21}\beta_{22}V_{1} + (-1 + sCR_{2}(\beta_{11} - 1) - \beta_{12}\beta_{21} - \beta_{11}(\beta_{32} - 1) + \beta_{32})V_{2}}{sCR_{1}R_{2} + R_{1}(1 - \beta_{32})}\gamma_{1},$$
(6)

$$I_2 = \frac{-\beta_{21}\beta_{22}V_1 + (1 - sCR_2(\beta_{11} - 1) + \beta_{12}\beta_{21} + \beta_{11}(\beta_{32} - 1) - \beta_{32})V_2}{sCR_1R_2 + R_1(1 - \beta_{32})}.$$
 (7)

## 3. Simulation results

To verify the theoretical results, the FIS circuits were simulated with SPICE program using 0.13  $\mu$ m IBM CMOS technology parameters (http://www.mosis.com/cgi-bin/cgiwrap/umosis/swp/params/ibm-013/t97f\_8hp\_5lm-params.txt), where  $\pm 0.75$  V DC power supply voltages and bias voltage  $V_B = 168$  mV were chosen. The DDCC in Figure 6 was derived from the structure reported in [29]. The dimensions of the CMOS transistors employed in DDCC structure are given in Table 1. Parasitic impedances of both proposed FISs are given in Table 2, where the passive components  $R_1 = R_2 = 1$  k $\Omega$  (X terminal parasitic resistor  $R_x = 80$   $\Omega$  is included) and C = 5 pF were chosen to obtain  $L_{eq} = CR_1R_2 = 5$   $\mu$ H.

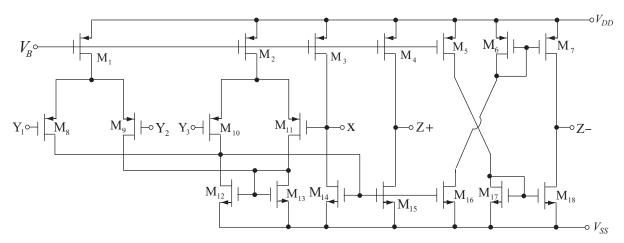


Figure 6. Internal structure of the DDCC derived from [29].

**Table 1.** Aspect ratios of the CMOS transistor of the DDCC in Figure 6.

PMOS transistors	$\mathrm{W}\;(\mu\mathrm{m})\;/\;\mathrm{L}\;(\mu\mathrm{m})$
$M_1 - M_{11}$	41.6/0.52
NMOS transistors	$\mathrm{W}~(\mu\mathrm{m})~/~\mathrm{L}~(\mu\mathrm{m})$
$M_{12}$ – $M_{18}$	4.55 / 0.52

Both ideal and simulated magnitudes and phases of the proposed FISs in Figures 2 and 3 are respectively shown in Figures 7 and 8, where the second terminals of the FISs are grounded (400 nH  $\leq L \leq$  10 mH). As an

•	
The first proposed FIS	The second proposed FIS
$r_s = 0.7 \Omega$	$r_s = 0.9 \Omega$
$R_{p1} = 12.7 \text{ k}\Omega$	$R_{p1} = 12.9 \text{ k}\Omega$
$R_{p2} = 9 \text{ k}\Omega$	$R_{p2} = 50.6 \text{ k}\Omega$
$C_{p1} = 168 \text{ fF}$	$C_{p1} = 155 \text{ fF}$
$C_{p2} = 138 \text{ fF}$	$C_{p2} = 310 \text{ fF}$

Table 2. Parasitic impedances of the proposed FISs.

example, the passive components  $R_1 = R_2 = 1 \text{ k}\Omega$  (X terminal parasitic resistor  $R_x = 80 \Omega$  is included) and C = 5 pF were chosen to obtain  $L_{eq} = CR_1R_2 = 5 \mu\text{H}$ . Additionally, the frequency performance comparison graph of the proposed FISs with the FIS given in [14] is given as an example in Figure 9. Time domain responses of FISs in Figures 2 and 3 are respectively given in Figures 10 and 11, where triangular-wave input currents are applied to obtain corresponding square-wave output voltages. Power dissipations of the FISs in Figures 2 and 3 were approximately 6.9 mW. A fourth-order band-pass filter example to demonstrate the performance of the proposed FISs is given in Figure 12. The transfer function (TF) of the fourth-order band-pass filter in Figure 12 is evaluated as

$$H(s) = \frac{V_{BP}}{V_{in}} = \frac{s\frac{R_1}{L_1}}{s^2 + s\frac{R_1}{L_1} + \frac{1}{L_1C_1}} \times \frac{s\frac{R_2}{L_2}}{s^2 + s\frac{R_2}{L_2} + \frac{1}{L_2C_2}},$$
 (8)

where angular resonance frequencies are computed as

$$\omega_{01} = \sqrt{\frac{1}{L_1 C_1}},\tag{9}$$

$$\omega_{02} = \sqrt{\frac{1}{L_2 C_2}}. (10)$$

Quality factors are found as follows:

$$Q_1 = \frac{1}{R_1} \sqrt{\frac{L_1}{C_1}},\tag{11}$$

$$Q_2 = \frac{1}{R_2} \sqrt{\frac{L_2}{C_2}}. (12)$$

As an example, the passive components  $R_1 = R_2 = 1 \text{ k}\Omega$  (X terminal parasitic resistor  $R_x = 80 \Omega$  is included) and C = 25 pF yielding  $L_1 = L_2 = CR_1R_2 = 25 \mu\text{H}$  are selected for both of the proposed FISs. Additionally,  $R_1 = R_2 = 1 \text{ k}\Omega$  and  $C_1 = C_2 = 100 \text{ pF}$  resulting in  $\omega_{o1} = \omega_{o2} = 20 \text{ Mrad/s}$  and  $Q_1 = Q_2 = 2 \text{ are chosen}$  for the fourth-order band-pass filter in Figure 12. The gain responses of the fourth-order band-pass filter in Figure 12 are shown in Figure 13 where the first and second proposed FISs are separately employed. The total harmonic distortion variations at f = 3.18 MHz versus applied peak values of the sinusoidal voltage signal are given in Figure 14, where the first and second proposed FISs are separately employed. It is observed from Figure 14 that the first proposed FIS employed in the filter has a good performance when compared to the second one. Output and input noises with respect to frequency are given in Figure 15, in which the first and second proposed FISs are separately employed. As an example, the passive components  $R_1 = R_2 = 1 \text{ k}\Omega$  with 10% variations and C = 5 pF were selected for both of the proposed FISs to perform Monte Carlo analysis with fifty runs. The results for the first and second FISs are respectively given in Figures 16 and 17.

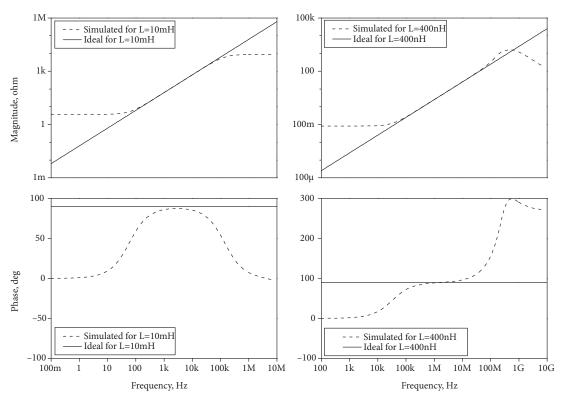


Figure 7. Impedance and phase of the floating inductor simulator in Figure 2 with respect to frequency.

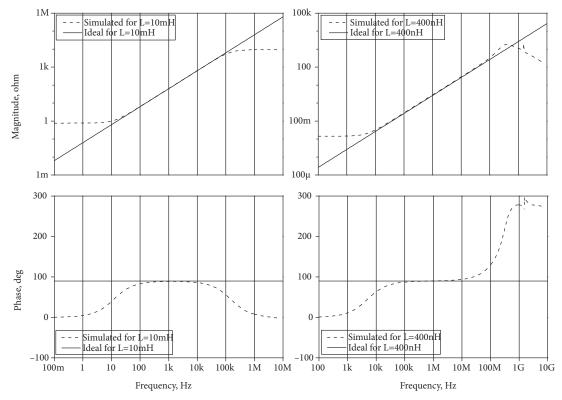


Figure 8. Impedance and phase of the floating inductor simulator in Figure 3 with respect to frequency.

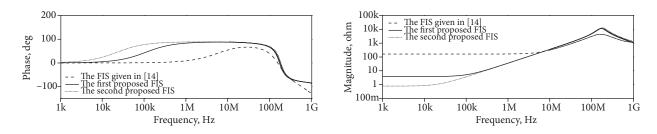


Figure 9. The comparison graph with FIS given in [14].

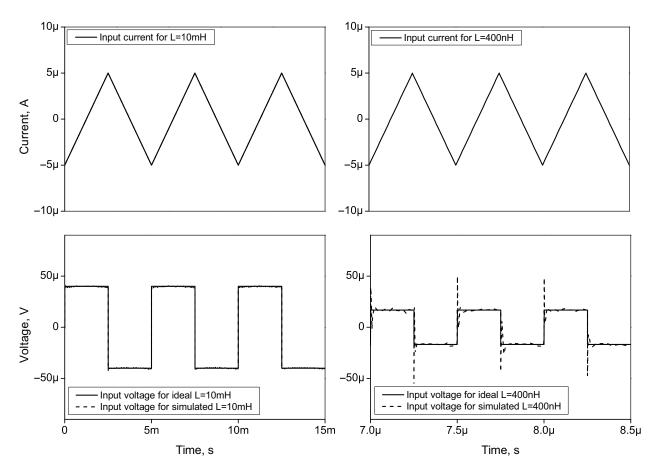


Figure 10. Ideal and simulated time domain responses of the floating inductor simulator in Figure 2.

Note that, as expected, simulation results agreed quite well with the theoretical ones. The discrepancy between ideal and simulated ones, however, mainly arises from nonideal gain and parasitic impedance effects of the DDCCs as well as signal limitations of the floating simulator configurations.

## 4. Stability analysis

Stability analysis was given for the filters in [35] and [36] before. Similarly, FISs have stability problems due to both poles and zeros of their impedances, which are affected by frequency-dependent nonideal gains [37]. In this paper, it is assumed that all the poles of frequency-dependent nonideal gains are sufficiently large; accordingly, their effects except DC gains are ignored. All the DC gains except  $\beta_{32}$  of the first proposed circuit are assumed

to be equal to unity. For the first proposed FIS, if  $\beta_{32} \leq 1$ , it is stable. Otherwise, it is unstable. However, if we replace the first proposed FIS in the second-order low-pass filter in Figure 18, the stability condition changes. Hence, the stability test for the second-order low-pass filter in Figure 19 is accomplished. Stability regions with respect to  $R_1$  and  $\beta_{32}$  are given in Figure 19. It is important to note that C=100 pF,  $R_2=1$  k $\Omega$ , and  $L=10^{-7}R_1$  H are chosen in Figure 18 to draw the stable and unstable regions in Figure 19.

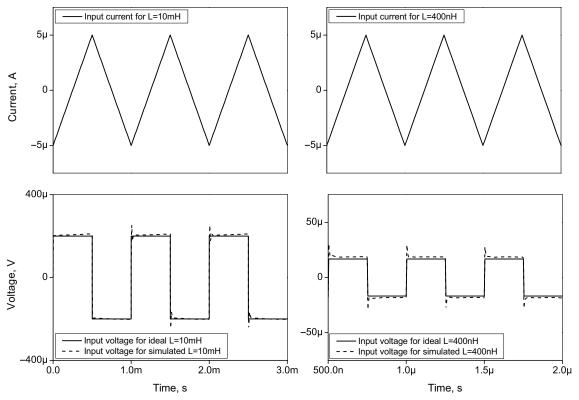
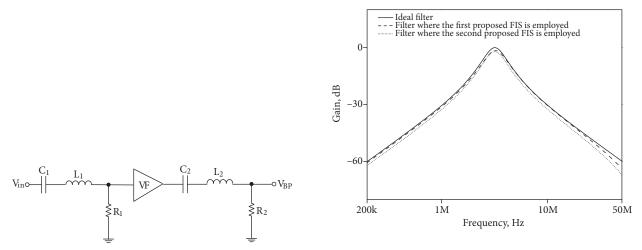
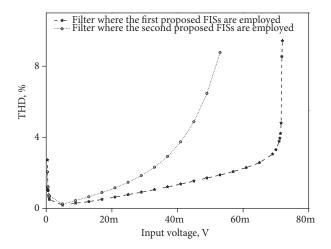


Figure 11. Ideal and simulated time domain responses of the floating inductor simulator in Figure 3.



**Figure 12.** Fourth-order band-pass filter example to show performance of the proposed FISs.

**Figure 13.** Gain responses of the fourth-order band-pass filter in Figure 11.

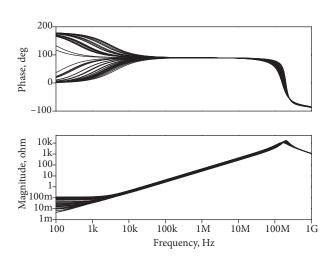


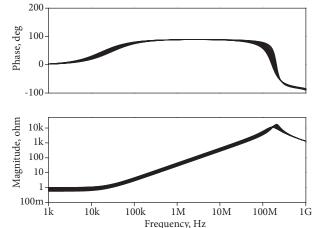
100n --- Output noise of the filter where the first FIS is employed Output noise of the filter where the second FIS is employed

10n --- Input noise of the filter where the first FIS is employed Input noise of the filter where the second FIS is employed Input noise of the filter where the second FIS is employed Input noise of the filter where the second FIS is employed Input noise of the filter where the second FIS is employed Input noise of the filter where the first FIS is

Figure 14. Total harmonic distortion variations at f = 3.18 MHz with respect to applied peak values of the sinusoidal voltage signals.

**Figure 15.** Output and input noises with respect to frequency.





**Figure 16.** Monte Carlo analysis for the first proposed FIS.

Figure 17. Monte Carlo analysis for the second proposed

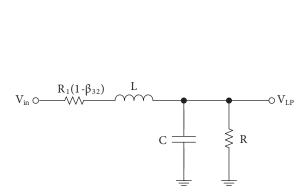
The TF of the filter in Figure 18 is calculated as:

$$H(s) = \frac{V_{LP}}{V_{in}} = \frac{\frac{1}{LC}}{s^2 + s\left(\frac{1}{RC} + \frac{R_1(1-\beta_{32})}{L}\right) + \frac{1}{LC}\left(1 + \frac{R_1(1-\beta_{32})}{R}\right)}.$$
 (13)

Here, the angular resonance frequency and quality factor are respectively evaluated as follows:

$$\omega_o = \sqrt{\frac{1}{LC} \left( 1 + \frac{R_1(1 - \beta_{32})}{R} \right)},\tag{14}$$

$$Q = \frac{\omega_o}{\frac{1}{RC} + \frac{R_1(1 - \beta_{32})}{L}}. (15)$$



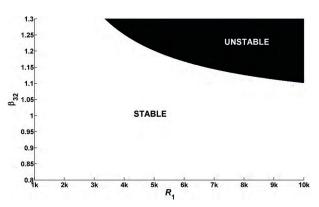


Figure 18. Second-order low-pass filter example for the stability test.

**Figure 19.** Stability regions with respect to  $R_1$  and  $\beta_{32}$ .

## 5. Conclusion

In this study, two new FIS circuits employing two DDCCs are given. Neither of the proposed configurations in this work suffer from critical passive component matching conditions and they both consist of a canonical number of passive elements. In addition to these, both of the proposed FISs contain a grounded capacitor; thus, they are suitable for IC fabrication. Simulations performed with the SPICE program confirmed the proposed theory. Furthermore, a stability test was performed for the first FIS used in a second-order low-pass filter in order to provide a way for the analog circuit designers to determine the parameters of the circuits.

## Acknowledgements

We would like to thank the anonymous reviewers and the associate editor for their invaluable comments for improving the paper.

## References

- [1] Ferri G, Guerrini NC. Low-Voltage Low-Power CMOS Current Conveyors. London, UK: Kluwer Academic Publishers, 2003.
- [2] Yuce E. On the implementation of the floating simulators employing a single active device. AEU International Journal of Electronics and Communications 2007; 61: 453–458.
- [3] Tangsrirat W. Floating simulator with a single DVCCTA. Indian J Eng Mater S 2013; 20: 79–86.
- [4] Sagbas M. Component reduced floating  $\pm L$ ,  $\pm C$  and  $\pm R$  simulators with grounded passive components. AEU International Journal of Electronics and Communications 2011; 65: 794–798.
- [5] Li Y. NAM expansion method for systematic synthesis of OTA-based floating gyrators. AEU International Journal of Electronics and Communications 2013; 67: 289–294.
- [6] Sagbas M, Ayten UE, Sedef H, Koksal M. Floating immittance function simulator and its applications. Circuits Syst Signal Process 2009; 28: 55–63.
- [7] Pal K. Modified current conveyors and their applications. Microelectr J 1989; 20: 37-40.
- [8] Sedef H, Acar C. A new floating inductor circuit using differential voltage current conveyors. Frequenz 2000; 54: 123–125.
- [9] Yuce E. On the realization of the floating simulators using only grounded passive components. Analog Integr Circ S 2006; 49: 161–166.

- [10] Pal K. Novel floating inductance using current conveyors. Electron Lett 1981; 17: 638.
- [11] Yuce E, Minaei S, Cicekoglu O. Resistorless floating immittance function simulators employing current controlled conveyors and a grounded capacitor. Electr Eng 2006; 88: 519–525.
- [12] Keskin AU, Erhan H. CDBA-based synthetic floating inductance circuits with electronic tuning properties. ETRI Journal 2005; 27: 239–241.
- [13] Ayten UE, Sagbas M, Herencsar N, Koton J. Novel floating general element simulators using CBTA. Radioengineering 2012; 21: 11–19.
- [14] Yuce E. A novel floating simulation topology composed of only grounded passive components. Int J Electron 2010; 97: 249–262.
- [15] Jaikla W, Siripruchyanun M. Realization of current conveyors-based floating simulator employing grounded passive elements. Proceedings of the 4th International Conference on Electrical Engineering/Electronics, Computer, Telecommunications and Information Technology (ECTI-CON); 2007. pp. 89–92.
- [16] Yuce E. Floating inductance, FDNR and capacitance simulation circuit employing only grounded passive elements. Int J Electron 2006; 93: 679–688.
- [17] Pal K. New inductance and capacitor floatation schemes using current conveyors. Electron Lett 1981; 17: 807-808.
- [18] Senani R, Bhaskar DR. New lossy/loss-less synthetic floating inductance configuration realized with only two CFOAs. Analog Integr Circ S 2012; 73: 981–987.
- [19] Senani R. On the realization of floating active elements. IEEE T Circuits Syst 1986; 33: 323–324.
- [20] Mohan PVA. Grounded capacitor based grounded and floating inductance simulation using current conveyors. Electron Lett 1998; 34: 1037–1038.
- [21] Yuce E, Cicekoglu O, Minaei S. CCII-based grounded to floating immittance converter and a floating inductance simulator. Analog Integr Circ S 2006; 46: 287–291.
- [22] Minaei S, Yuce E, Cicekoglu O. A versatile active circuit for realising floating inductance, capacitance, FDNR and admittance converter. Analog Integr Circ S 2006; 47: 199–202.
- [23] Yuce E, Cicekoglu O, Minaei S. Novel floating inductance and FDNR simulators employing CCII+s. J Circuit Syst Comp 2006; 15: 75–81.
- [24] Kiranon W, Pawarangkoon P. Floating inductance simulation based on current conveyors. Electron Lett 1997; 33: 1748–1749.
- [25] Senani R. Generation of new two-amplifier synthetic floating inductors. Electron Lett 1987; 23: 1202–1203.
- [26] Horng JW. Lossless inductance simulation and voltage-mode universal biquadratic filter with one input and five outputs using DVCCs. Analog Integr Circuit S 2010; 62: 407–413.
- [27] Yuce E, Minaei S. Novel floating simulated inductors with wider operating-frequency ranges. Microelectr J 2009; 40: 928–938.
- [28] Minaei S, Cicekoglu O, Kuntman H, Turkoz S. Electronically tunable active floating inductance simulation. Int J Electron 2002; 89: 905–912.
- [29] Chiu W, Liu SI, Tsao HW, Chen JJ. CMOS differential difference current conveyors and their applications. IEEE P-Circ Dev Syst 1996; 143: 91–96.
- [30] Sun Y. Design of high frequency integrated analogue filters. IET Circ Device Syst 2002; 14: 10.
- [31] Bhusan M, Newcomb RW. Grounding of capacitors in integrated circuits. Electron Lett 1967; 3: 148-149.
- [32] Prommeee P, Somdunyakanok M. CMOS-based current-controlled DDCC and its applications to capacitance multiplier and universal filter. AEU International Journal of Electronics and Communications 2011; 65: 1–8.
- [33] Yuce E, Minaei S. Universal current-mode filters and parasitic impedance effects on the filter performances. Int J Circ Theor App 2008; 36: 161–171.

## YUCE et al./Turk J Elec Eng & Comp Sci

- [34] Minaei S, Yuce E. A simple CMOS-based inductor simulator and frequency performance improvement techniques. AEU International Journal of Electronics and Communications, 2012; 66: 884–891.
- [35] Yuce E, Tokat S, Minaei S, Cicekoglu O. Stability problems in universal current-mode filters. AEU International Journal of Electronics and Communications 2007; 61: 580–588.
- [36] Yuce E, Tokat S. Design and stability analysis of mixed-mode filters containing only grounded capacitors. J Circuit Syst Comp 2010; 19: 1345–1363.
- [37] Yuce E, Cicekoglu O. The effects of non-idealities and current limitations on the simulated inductances employing current conveyors. Analog Integr Circ S 2006; 46: 103–110.