For cited: Anavatan, A. & Yalçın Kayacan, E. (2019). Are Bitcoin Returns Predictable?. Journal of Current Researches on Business and Economics, 9 (1), 13-22.



### http://dergipark.gov.tr/jocrebe

## Are Bitcoin Returns Predictable?\*

#### Aygül ANAVATAN<sup>1</sup> & Eda YALÇIN KAYACAN<sup>2</sup>

Abstract

#### Keywords Bitcoin, log-normal stochastic volatility model, stochastic

volatility model

with leverage,

leverage effect.

Article History

Received

12 Feb, 2019

Accepted

20 Mar, 2019

Bitcoin is the most radical of the cryptocurrencies which are becoming popular nowadays. The advantage of the cryptocurrencies is that they are decentralized systems so do not need central banks. The purpose of this study is to determine if there is a volatility in the returns of Bitcoin and if so, whether it is predictable. The volatility of the Bitcoin returns was investigated using the log-normal stochastic volatility model and stochastic volatility model with leverage for daily data covering the period between 19.12.2011 and 29.01.2018. While there is no significant leverage effect in the Bitcoin returns, it has been revealed that the volatility is permanent and unpredictable. The unpredictability of Bitcoin returns' fluctuations suggests that it is risky to use it as an investment tool or currency. It is increasing day by day that Bitcoin takes place of banknotes or digital money, which are conventional means of payment. The more widespread the system, the safer and the more resistant to speculations it is. The widespread popularity of Bitcoin may facilitate its recognition by states and inclusion in traditional payment methods.

# Bitcoin Getirileri Öngörülebilir Mi?\*

#### Anahtar Kelimeler

Bitcoin, log-normal stokastik oynaklık modeli, kaldıraçlı stokastik oynaklık modeli, kaldıraç etkisi.

#### Özet

Bitcoin, günümüzde popüler olan kripto para birimlerinin en köklüsüdür. Kripto para birimlerinin avantajı, ademi merkeziyetçi olmalarıdır, dolayısıyla merkez bankalarına ihtiyaç duymazlar. Bu çalışmanın amacı Bitcoin getirilerinde oynaklık olup olmadığını ve eğer varsa, öngörülebilir olup olmadığını belirlemektir. Bitcoin getirilerinin oynlıklığı, log-normal stokastik oynaklık modeli ve kaldıraçlı stokastik oynaklık modeli kullanılarak 19.12.2011 ve 29.01.2018 dönemini kapsayan günlük veriler için incelenmiştir. Bitcoin getirilerinde anlamlı bir kaldıraç etkisi bulunmaakla birlikte, oynaklığın kalıcı ve öngörülemez olduğu bulunmuştur. Bitcoin getiri dalgalanmaların öngörülememesi, onun bir yatırım aracı veya para birimi olarak kullanılmasının riskli olduğunu göstermektedir. Bitcoin'in, geleneksel ödeme şekli olan banknotlar veya dijital paraların yerini alması gün geçtikçe

<sup>\*</sup>This study is an extended version of the proceeding which was presented at 25th The Eurasia Business and Economics Society (EBES) conference.

<sup>&</sup>lt;sup>1</sup> Corresponding Author. ORCID: 0000-0003-0130-9555. Assist. Prof. Dr., Pamukkale University, Faculty of Business and Administarive Sciences, Department of Econometrics, aanavatan@pau.edu.tr

<sup>&</sup>lt;sup>2</sup> Corresponding Author. ORCID: 0000-0002-1616-9121. Dr., Pamukkale University, Faculty of Business and Administarive Sciences, Department of Econometrics, eyalcin@pau.edu.tr

Makale Geçmişi Alınan Tarih 12 Şubat 2019 Kabul Tarihi 20 Mart 2019 artmaktadır. Sistem ne kadar yaygın olursa, o kadar güvenli ve spekülasyonlara o kadar dirençli olmaktadır. Bitcoin'in yaygın popülaritesi, onun devletler tarafından tanınmasını ve geleneksel ödeme yöntemlerine dahil edilmesini kolaylaştırabilir.

## 1. Introduction

Bitcoin is the most popular of the 897 cryptocurrencies as of February 2018. It is the first cryptocurrency proposed by Nakamoto (2008) and was released as opensource software in 2009. Bitcoin works with Blockchain technology, one of the world's leading software platforms for digital assets. The most important feature of cryptocurrencies is that they are decentralized and that central banks are not needed in this mechanism. As the world has never seen such a fictional currency, it's really exciting to imagine how the cryptocurrencies will advance. In this study, our aim is to determine if there is volatility in the Bitcoin returns and if so, whether it is predictable.

In the related literature, Bech & Garratt (2017) suggest the central bank cryptographic currency concept. Nagpal (2018), explains the emergence, functioning, and risks of digital money.

Baur & Dimpfl (2017) examine the volatility of four different Bitcoin markets by comparing US dollar, the euro and the Japanese yen via fractional integration and Granger causality tests. Eross, Mcgroarty, Urquhart, & Wolfe (2017) investigate the relationship between returns, volume, bid-ask spread (BAS) and volatility of Bitcoin by using Granger causality. Chengyuan (2017) analyzes the volatility transmission of Bitcoin price between Chinese and US markets through the Granger causality test and the BEKK model. Urquhart (2018) ascertains the relationship between realized volatility and volume of Bitcoin and investor attention by way of Vector Autoregression, Granger causality and Impulse Response analysis. Ciaian, Rajcaniova, & Kancs (2018) examine interdependencies between Bitcoin and 16 altcoin markets in the short- and long-run by using Autoregressive Distributed Lag (ARDL) model.

Fiser (2015) analyzes Bitcoin bubbles using ARIMA, GARCH and Log-Periodic Power Law model (LPPL) models. Kasper (2017) compares Bitcoin volatility to volatility of currencies of least developed countries and other cryptocurrencies by GARCH model. Stavroyiannis (2017) investigates volatility dynamics of the six major digital currencies, Bitcoin, Ethereum, Ripple, Litecoin, Dash, and NEM, using GARCH models. Corbet, Larkin, Lucey, Meegan, & Yarovaya (2017) examine the reaction of 100 digital assets to US policy announcements by use of GARCH model. Cermak (2017) researches whether Bitcoin is a useful currency by using GARCH model. Liu, Shao, & Wei (2017) compare the empirical performance of a standard normal distribution, the Student's t distribution and the normal reciprocal inverse Gaussian (NRIG) for the daily Bitcoin exchange rate returns via GARCH model. Bouri, Azzi, & Dyhrberg (2018) investigate the return-volatility relationship for Bitcoin using the asymmetric GARCH model both before and after the price crash of 2013 and throughout the study period. Shi (2018) examines the effect of Bitcoin futures on the volatility and liquidity of the Bitcoin spot market through the asymmetric EGARCH model with a generalized error distribution (GED).

Cheah & Fry (2015) investigate whether there are the bubbles in Bitcoin markets by using a stochastic bubble model. Catania & Grassi (2017) use 289 cryptocurrencies and focus on four of them, Bitcoin, Ethereum, Ripple, and Litecoin, and extend Score-Driven GHSKT model considering the properties of long memory, leverage effect and time-varying higher order moments. Balcilar, Bouri, Gupta, & Roubaud (2017) examine the causality relationship between Bitcoin returns, volatility and trading volume by considering nonlinearity and structural breaks via a non-parametric causality-in- quantiles test. Lahmiri & Bekiros (2018) reveal the chaos, randomness, and multi-fractality in Bitcoin prices and returns which are separated into the low regime and high regime by using the largest Lyapunov exponent, Shannon entropy, and the multi-fractal detrended fluctuation analysis.

Johnson (2017) estimates stochastic volatility (SV) models with heavy tails, leverage, and covariates by using particle Markov Chain Monte Carlo (MCMC) method for Bitcoin exchange rate data. Johnson (2017) analyzes the volatility of the Bitcoin returns using the SV models. The rest of the study has been organized as follows. Section 2 presents the methodology related to log-normal SV model and SV model with leverage. Section 3 introduces the dataset used in the analysis and reports the empirical results. Finally, Section 4 concludes.

# 2. Methodology

The studies in order to model the volatility are based on Clark (1973). The increases in the price process  $\Delta x_t = x_t - x_{t-1}$  are stationary in the mean and uncorrelated, where  $x_t$  indicates the price at time t. This situation can best be explained by a random walk as follows (Clark, 1973: 135);

$$x_t = x_{t-1} + \varepsilon_t, E(\varepsilon_t) = 0, E(\varepsilon_t \varepsilon_s) = 0, \text{ for } t \neq s$$
(1)

Clark (1973) laid the foundations for the SV model by modelling the  $\sigma^2$  process, which is the variance of  $\varepsilon_t$ . There are several models in which variance and covariance change. The basis of models in which volatility is defined as an observable and deterministic variable is the autoregressive conditional variance (ARCH) model proposed by Engle (1982). The first order autoregressive model can be written as follows;

$$Y_t = \gamma Y_{t-1} + \varepsilon_t \tag{2}$$

where  $Y_t$  is a random variable drawn from the conditional density function  $f(Y_t|Y_{t-1})$ ,  $\varepsilon_t$  is the white noise process which has the variance  $\sigma^2$ . The conditional mean and unconditional mean of  $Y_t$  are  $\gamma Y_{t-1}$  and zero, respectively. The conditional variance of  $Y_t$  is  $\sigma^2$  while the unconditional variance is  $\sigma^2/1 - \gamma^2$ . The bilinear model which allows the conditional variance to depend on the past realization of the series is as follows (Engle, 1982: 987-988);

 $Y_t = \varepsilon_t Y_{t-1} \quad (3)$ 

where the conditional variance is  $\sigma^2 Y_{t-1}^2$ . However, the unconditional variance is zero or infinite. Despite the fact that this problem is avoided with light measures, this is an undesirable situation. An ARCH model is defined as follows (Engle, 1982: 988);

$$Y_t = \varepsilon_t h_t^{1/2} \quad (4)$$
$$h_t = \alpha_0 + \alpha_1 Y_{t-1}^2 \quad (5)$$

where  $var(\varepsilon_t) = 1$ . In this model, the variance in time t is allowed to be a linear function of the squares of past observations. The generalized form of this model can be stated as in (6) (Engle, 1982: 988);

$$h_t = \alpha_0 + \alpha_1 Y_{t-1}^2 + \dots + \alpha_p Y_{t-p}^2$$
 (6)

Taylor (1982), proposed an SV model that allows the volatility to be a function of the unobserved or latent component in parameter-based or state-space models. The volatility, which can be observed and modeled as a deterministic variable in ARCH-GARCH models, has an unobservable and stochastic structure in SV models. The volatility in SV models is determined by an unpredictable shock. While the conditional mean has a stochastic process in ARCH-GARCH models, both the conditional mean and the conditional variance follow the stochastic process in the SV models (Göktaş & Hepsağ, 2016: 4).

Classical SV model is defined as follows (Taylor, 2008: 74);

$$y_t = \varepsilon_t \exp(h_t/2), \varepsilon_t \sim N(0,1)$$
(7)  
$$h_t = \gamma + \phi h_{t-1} + \eta_t, \eta_t \sim N(0, \sigma_\eta^2)$$
(8)

where is assumed that  $\varepsilon_t$  and  $\eta_t$  are mutually independent and identically distributed (iid) random variables.  $h_t$  refers to the unobservable volatility. (7) and (8) are the mean and volatility equation, respectively. Because of the Gaussianity of  $\eta_t$ , this model is called as log-normal SV model.  $\phi$  indicates the continuity (permanence) of the volatility. If  $\phi$  is close to 1, it can be concluded the existence of volatility clustering in the data.  $\sigma_{\eta}$  also indicates the variability of volatility. If  $\sigma_{\eta}^2$  is close to 0, it can be expressed that the volatility is predictable (Göktaş & Hepsağ, 2016: 11).

The SV model with dynamic leverage effect, including the asymmetric relations due to the direct negative correlation between the changes in volatility, and returns, is as follows (Asai & McAleer, 2005: 320);

$$y_{t} = \varepsilon_{t} \exp(h_{t}/2), \varepsilon_{t} \sim N(0,1)$$
(9)  
$$h_{t+1} = \mu + \varphi h_{t} + \eta_{t}, \eta_{t} \sim N(0,\sigma_{\eta}^{2})$$
(10)  
$$E(\varepsilon_{t},\eta_{t}) = \rho \sigma_{\eta}$$
(11)

While it is assumed that  $\varepsilon_t$  and  $\eta_t$  are mutually independent in SV models,  $\varepsilon_t$  and  $\eta_t$  are allowed to be the contemporaneous relationship in SV models with dynamic leverage effect. In this case, the relationship becomes asymmetric (Ghysels, Harvey, & Renault, 1996: 139).  $\rho$  is the relationship between the variation in volatility, and return series, and can be stated as  $corr(\varepsilon_t, \eta_t) = \rho$ . If  $\rho$  is negative, the negative changes in  $\varepsilon_t$  cause the higher volatility in contemporaneous and following periods. On the other hand, positive changes in  $\varepsilon_t$  are associated with decreases in volatility. That is, when  $\rho$  is negative, negative shocks increase the fluctuation more than positive shocks. This asymmetry is called as leverage effect (Jacquier, Polson, & Rossi, 2004: 193).

As the time dimension increases or the dimension of  $h_t$  goes above 1, the sample size grows (Shephard, 1996: 28). Because the sample size is often large and no traditional integral technique can be used to estimate the model, the Bayesian method MCMC procedure is used to estimate SV model and SV model with dynamic leverage effect (Danielsson, 1994: 376). In the MCMC method, parameters are estimated using Gibbs or Metropolis sampling.

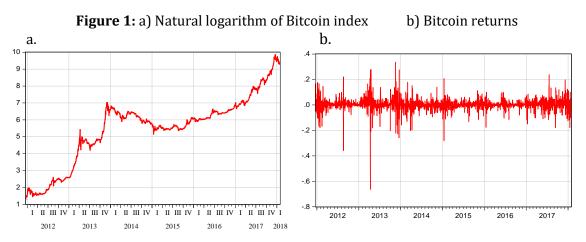
# 3. Dataset and Empirical Results

In this study, volatility behavior of Bitcoin returns for closing prices is investigated using SV and SV with dynamic leverage effect. The Bitcoin price index is taken in USD-denominated for the period between 19.12.2011 and 29.01.2018 on Bitstamp, which is obtained from www.bitcoincharts.com. Bitstamp is the most rooted European Bitcoin exchange and dates back 2011, also mainly focus on trading Bitcoin. Table 1 reports the descriptive statistics for the return of the Bitcoin index for 2234 observations.

Table 1: Descriptive statistics								
Mean	Median	Minimum	Maximum	Standard Deviation	Skewness	Kurtosis	Jarque- Bera	Probability
0.003613	0.002553	-0.663948	0.337486	0.048971	-1.365440	26.41153	51713.13	0.0000

Considering the descriptive statistics of the Bitcoin returns, it is observed that the mean value of the return series is smaller than the standard deviation. This situation is consistent with the fact that the financial time series generally follow the random walk process. It is seen that the series of returns are negative skewed and has higher kurtosis than normal distribution. The Jarque-Bera test statistic also shows that the distribution of return series is not normal. By virtue of these features, it can be stated that the Bitcoin index carries the typical financial time series feature.

The natural logarithm of the data and the return series for the bitcoin index, are presented in Figure 1. It is clear that there is an increasing trend in the bitcoin returns and that there are volatility clusters in the return series.



The preliminary distributions for the parameters to be estimated using the Gibbs sampler in the estimation of SV model and SV model with dynamic leverage effect were obtained from the codes used in the studies performed by Yasuhiro Omori. In the estimates made using the WinBUGS 1.4.3 package program, the initial values for the estimation method were determined by the package program and 100,000 samples were made.

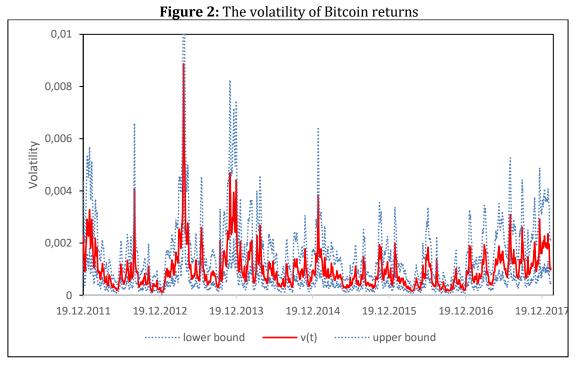
Table 2 reports the results of the estimated log-normal SV model for the Bitcoin returns.

	Coefficient	Standard Deviation	MC Error	Confidence Interval
μ	-7.263*	0.1755	0.005369	(-7.604, -6.908)
φ	0.9243*	0.01364	4.193E-4	(0.8964, 0.9488)
$\sigma_{\eta}$	0.5865*	0.0469	0.001607	(0.4975, 0.6796)

Note: \* denotes the rejection of the null hypothesis at the 5% significance level.

According to the estimation results of SV model shown in Table 2, the  $\varphi$  coefficient indicating the permanence of Bitcoin volatility is statistically significant at 5% significance level and is obtained as 0.9243. It is understood that the volatility is permanent and volatility clusters have arisen in Bitcoin returns take part in the Bitstamp market. The  $\sigma_n$  coefficient indicating the variability of the volatility is also statistically significant at the 5% significance level and is obtained as 0.5865 (  $\sigma_n^2 = 0.3440$ ). Accordingly, there is a high level of variability in Bitstamp market volatility. Given the fact that the  $\sigma_n^2$  coefficient is not close to 0, it can be made the interpretation that the volatility is not predictable. To sum up, it can be said that the volatility is permanent, the variability of the volatility is high and the volatility is not predictable.

Figure 2 shows the graph of estimated volatility values obtained from the model results belongs to Bitcoin returns. It is observed that the return volatility on 11.04.2013 is the highest level. It may be the cause of this volatility that the intense demand for Bitcoin, which has reached its highest closing price on 10.04.2013, was locked the system and not allowed new purchases for three days (www.bitstamp.net). It is also seen that the return volatility is at the lowest level on 28.12.2012.



The estimation results for the SV model with dynamic leverage effect belongs to the Bitcoin returns are given in Table 3.

	Table 5. The results of the estimated 57 model with dynamic reverage effect							
	Coefficient	Standard Deviation	MC Error	<b>Confidence Interval</b>				
μ	-7.229*	0.1684	0.00532	(-7.568, -6.923)				
$\phi$	0.9233*	0.01293	6.46E-04	(0.8975, 0.9472)				
ρ	-0.02426	0.04674	0.001848	(-0.1186, 0.06251)				
$\sigma_{\varepsilon}$	0.02703*	0.002259	7.21E-05	(0.02273, 0.03139)				
$\sigma_\eta$	0.5883*	0.04543	0.002126	(0.5037, 0.6831)				
$\sigma_{\eta}$	0.5883*	0.04543	0.002126	(0.5037, 0.6831)				

Table 3: The results of the estimated SV model with dynamic leverage effect

Note: \* denotes the rejection of the null hypothesis at the 5% significance level.

According to the estimation results of SV model with dynamic leverage effect shown in Table 3, the  $\varphi$  coefficient indicating the permanence of Bitcoin volatility is statistically significant at 5% significance level and is obtained as 0.9233. It is understood that the volatility is permanent and volatility clusters have arisen in Bitcoin returns take part in the Bitstamp market. The  $\sigma_{\eta}$  coefficient indicating the variability of the volatility is also statistically significant at the 5% significance level and is obtained as 0.5883 ( $\sigma_{\eta}^2 = 0.3461$ ). Accordingly, there is a high level of variability in Bitstamp market volatility. Given the fact that the  $\sigma_{\eta}^2$  coefficient is not close to 0, it can be made the interpretation that the volatility is not predictable. To sum up, it can be said that the volatility is permanent, the variability of the volatility is not predictable. These findings are consistent with those of the log-normal SV model. The  $\rho$  coefficient indicating the relationship between Bitcoin returns and the changes in the volatility is not statistically significant at the 5% significance level. For this reason, it cannot be said that the leverage effect exists in Bitcoin returns.

## 4. Conclusion

SV models are used in order to model time series data, especially in financial applications. The motivation for this study is to determine if there is volatility in the Bitcoin returns and if so, whether it is predictable. Although the use of Bitcoin is now not popular enough to have a huge impact on the real economy, it is worth to examine in terms of understanding the trajectory of cryptocurrencies.

In this study, it is found that the volatility is permanent in Bitcoin returns, the variability of the volatility is high, and the volatility is not predictable. Also, there is no leverage effect, which refers to the asymmetric reaction of the volatility process to past positive and negative returns, on Bitcoin returns. The unpredictability of Bitcoin fluctuations suggests that it is risky to use it as an investment tool or currency. This study revealed that Bitcoin returns were risky and unpredictable by using econometric techniques. If the volatility in Bitcoin returns were found to be predictable, it would be appropriate to make future estimations using various forecasting techniques.

This study can be developed by examining other cryptocurrencies with SV models or searching the volatility of Bitcoin returns with other methods. In addition, the presence of structural breaks or regime changes in the analysis can also be taken into account.

## References

- Asai, M., & McAleer, M. (2005). Dynamic asymmetric leverage in stochastic volatility models. Econometric Reviews, 24(3), 317–332.
- Balcilar, M., Bouri, E., Gupta, R., & Roubaud, D. (2017). Can volume predict Bitcoin returns and volatility? A quantiles-based approach. Economic Modelling, 64, 74–81.
- Baur, D. G., & Dimpfl, T. (2017). Realized Bitcoin Volatility. SSRN Electronic Journal, 1–25. Retrieved from https://www.ssrn.com/abstract=2949754
- Bech, M., & Garratt, R. (2017). Central bank cryptocurrencies. BIS Quarterly Review, September, 55–70.
- Bouri, E., Azzi, G., & Dyhrberg, A. H. (2018). On the return-volatility relationship in the Bitcoin market around the price crash of 2013. SSRN Elecronic Journal, 1–20. Retrieved from https://ssrn.com/abstract=2869855
- Catania, L., & Grassi, S. (2017). Modelling Crypto-Currencies Financial Time-Series. SSRN Elecronic Journal, 1–38. Retrieved from https://ssrn.com/abstract=3028486
- Cermak, V. (2017). Can Bitcoin Become a Viable Alternative to Fiat Currencies? An Empirical Analysis of Bitcoin's Volatility Based on a GARCH Model. SSRN Electronic Journal, 1–52. Retrieved from http://www.ssrn.com/abstract=2961405

- Cheah, E.-T., & Fry, J. (2015). Speculative bubbles in Bitcoin markets? An empirical investigation into the fundamental value of Bitcoin. Economics Letters, 130, 32–36.
- Chengyuan, Q. (2017). BitCoin in China: Price Discovery and Volatility Transmission. SSRN Elecronic Journal, 1–13. Retrieved from https://ssrn.com/abstract=2934031
- Ciaian, P., Rajcaniova, M., & Kancs, D. (2018). Virtual relationships: Short- and longrun evidence from BitCoin and altcoin markets. Journal of International Financial Markets, Institutions and Money, 52, 173–195.
- Clark, P. K. (1973). A Subordinated Stochastic Process Model with Finite Variance for Speculative Prices. Econometrica, 41(1), 135–155.
- Corbet, S., Larkin, C., Lucey, B., Meegan, A., & Yarovaya, L. (2017). Cryptocurrency reaction to FOMC Announcements: Evidence of Heterogeneity Based on Blockchain Stack Position. SSRN Elecronic Journal, 1–39. Retrieved from https://ssrn.com/abstract=3073727
- Danielsson, J. (1994). Stochastic volatility in asset prices: Estimation with simulated maximum likelihood. Journal of Econometrics, 64, 375–400.
- Engle, R. F. (1982). Autoregressive Conditional Heteroscedasticity with Estimates of the Variance of United Kingdom Inflation. Econometrica, 50(4), 987–1007.
- Eross, A., Mcgroarty, F., Urquhart, A., & Wolfe, S. (2017). The Intraday Dynamics of Bitcoin. SSRN Elecronic Journal, 1–24.
- Fiser, P. (2015). Econometric Analysis of Bitcoin and its 2013 Bubbles. Charles University in Prague.
- Ghysels, E., Harvey, A. C., & Renault, E. (1996). Stochastic Volatility. In G. S. Maddala & C. R. Rao (Eds.), Handbook of Statistics 14: Statistical Methods in Finance (pp. 119–191). Amsterdam: Elsevier B.V.
- Göktaş, Ö., & Hepsağ, A. (2016). BIST-100 Endeksinin Volatil Davranışlarının Simetrik Ve Asimetrik Stokastik Volatilite Modelleri ile Analizi. Ekonomik Yaklaşım, 27(99), 1–15.
- Jacquier, E., Polson, N. G., & Rossi, P. E. (2004). Bayesian analysis of stochastic volatility models with fat-tails and correlated errors. Journal of Econometrics, 122(1), 185–212.
- Johnson, M. (2017). Analysis of the Bitcoin Exchange Using Particle MCMC Methods. Simon Fraser University.
- Kasper, J. (2017). Evolution of Bitcoin: Volatility Comparisons with Least Developed Countries' Currencies. SSRN Elecronic Journal, 1–22. Retrieved from https://ssrn.com/abstract=3052207
- Lahmiri, S., & Bekiros, S. (2018). Chaos, randomness and multi-fractality in Bitcoin market. Chaos, Solitons and Fractals, 106, 28–34.

Journal of Current Researches on Business and Economics, 2019, 9 (1), 13-22.

- Liu, R., Shao, Z., & Wei, G. (2017). Volatility clustering, fat tails and Bitcoin exchange rate returns. SSRN Elecronic Journal, 1–9. Retrieved from https://ssrn.com/abstract=3015077
- Nagpal, S. (2018). Cryptocurrency: The Revolutionary Future Money. SSRN Elecronic Journal. Retrieved from https://ssrn.com/abstract=3090813
- Nakamoto, S. (2008). Bitcoin: A Peer-to-Peer Electronic Cash System, 1–9. Retrieved from https://bitcoin.org/bitcoin.pdf
- Shephard, N. (1996). Statistical aspects of ARCH and stochastic volatility. In D. R. Cox, D. V. Hinkley, & O. E. Barndorff-Nielsen (Eds.), Time Series Models in Econometrics, Finance and Other Fields (1st ed., p. 225). Springer-Science+Business Media, B.V.
- Shi, S. (2018). The Impact of Futures Trading on Intraday Spot Volatility and Liquidity: Evidence from Bitcoin Market. SSRN Elecronic Journal, 1–14. Retrieved from https://ssrn.com/abstract=3094647
- Stavroyiannis, S. (2017). Volatility Modeling and Risk Assessment of the Major Digital Currencies. SSRN Elecronic Journal, 1–11. Retrieved from https://ssrn.com/abstract=3092173
- Taylor, S. J. (1982). Financial Returns Modelled by the Product of Two Stochastic Processes—A Study of Daily Sugar Prices, 1961–79. In N. Shephard (Ed.), Stochastic Volatility: Selected Readings (pp. 60–82). New York: Oxford University Press.
- Taylor, S. J. (2008). Modelling Financial Time Series (Second). New York: Wiley.
- Urquhart, A. (2018). What Causes the Attention of Bitcoin? SSRN Elecronic Journal, 1–12. Retrieved from https://ssrn.com/abstract=3097153
- www.bitcoincharts.com. (2018). Retrieved January 29, 2018, from www.bitcoincharts.com
- www.bitstamp.net. (2018). Retrieved February 1, 2018, from https://www.bitstamp.net/article/ overwhelming-popularity/

# E-ISSN: 2547-9628 Strategic Research Academy ©

© Copyright of Journal of Current Researches on Business and Economics is the property of Strategic Research Academy and its content may not be copied or emailed to multiple sites or posted to a listserv without the copyright holder's express written permission. However, users may print, download, or email articles for individual use.