

Filo Büyüklüğü ve Karma Araç Rotalama Problemleri İçin Yeni Bir Yapısal Rotalama Algoritması

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(Alınış Tarihi: 24.01.2014, Kabul Tarihi: 04.07.2014)

Anahtar Kelimeler

Filo Büyüklüğü ve Karma Araç Rotalama Problemi Yapısal Sezgiseller Araç Rotalama Problemi Rotalama Algoritmaları Ochi Rotalama Algoritması. **Özet:** Bu çalışmada, Filo Büyüklüğü ve Karma Araç Rotalama Problemleri için yeni bir yapısal rotalama yaklaşımı önerilmiştir. Önerilen yaklaşım Ochi rotalama yaklaşımı ile matematiksel olarak benzerlik göstermesine rağmen, tamamen farklı ve yeni bir yaklaşımdır. Çünkü bu yaklaşım araç tiplerini yani kapasitelerini dikkate alırken, Ochi yaklaşımı boş kalan kapasitenin maliyetlerini dikkate almaktadır. Önerilen yeni rotalama yaklaşımı ve Ochi rotalama yaklaşımlarına ilişkin

algoritmalar verilmiştir. Örnek bir problem ile verilen rotalama yaklaşımlarının çözüm aşamaları detaylı bir şekilde anlatılmıştır. Örnekte rasgele seçilen bireyler için algoritmalardan farklı rotalar ve farklı maliyetler elde edilmiştir. Önerilen yeni yaklaşımla daha düşük maliyetli rotaların elde edildiği görülmüştür. Ancak örnek problem üzerindeki çalışmaların yeterli olmayacağı düşünülerek Golden'ın 12 test problemi (Sabit Maliyetli Filo Büyüklüğü ve Karma Araç Rotalama Problemi) üzerinde bu rotalama yaklaşımları karşılaştırılmıştır. Golden'ın test problemlerinde ortalama zaman karmaşıklığı ve ortalama çözüm performansı açısından önerilen yeni yaklaşımın üstünlüğü ortaya çıkmıştır. Böylece önerilen yaklaşımın, Sabit Maliyetli Filo Büyüklüğü ve Karma Araç Rotalama Problemleri için farklı ve yeni bir yaklaşım olduğu sonucuna varılmıştır.

A Novel Constructive Routing Algorithm for Fleet Size and Mix Vehicle Routing Problem

Keywords

Fleet Size and Mix Vehicle Routing Problem Constructive Heuristics Vehicle Routing Problem Routing Algorithms Ochi's Routing Approach.

Abstract: In this study, a new constructive routing algorithm for fleet size and mix vehicle routing problem is proposed in which residual costs rather than vehicle types are considered for route selection.

The algorithm of the proposed routing approach is given and then the solution phases of a sample problem are shown by using the given algorithm. In order to highlight the performance of the routing approach, Golden's 12 test problems (Fleet Size and Mix Vehicle Routing Problem with Fixed Cost) are used. It is seen that the proposed method has better average time complexity and cost performances than Ochi's routing approach. Therefore, the solutions of the proposed method that uses vehicle type information are better than those of the methods that use residual cost based on the vehicle type information.

1. Introduction

In fleet size and mix vehicle routing problem (HFVRP) each customer is visited by exactly one route. HFVRP consists of designing a number of feasible paths having minimum total cost / total distance. Aim of HFVRP is mainly to determine the best fleet composition as well as the set of paths that minimize the sum of fixed and travel costs in such a way that:

(a) every route starts and ends at the depot and is associated to a vehicle type;

(b) each customer belongs to exactly one route; and (c) the vehicle's capacity is not exceeded.

The HFVRP is an NP-hard problem and numerous methods have been proposed as it is a natural generalization of the travelling salesman problem (TSP) and as it includes the classical vehicle routing problem (VRP) (Ochi et al., 1998; Lima et al., 2004; Baldacci et al., 2008; Subramanian et al., 2012).

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Some researchers developed algorithms such as the savings algorithm of Clarke and Wright (Clarke and Wright, 1964), the sweep algorithm of Gillett and Miller (Gillett and Miller, 1974) and the generalized assignment of Fisher and Jaikumar (Fisher and Jaikumar, 1981). Matching based saving algorithms were also proposed by Desrochers and Verhoog (Desrochers and Verhoog, 1991), Salhi and Rand (Salhi and Rand, 1993) and Osman and Salhi (Osman and Salhi, 1996). Evolutionary algorithms have been attempted by Ochi et al. (Ochi et al., 1998) and Lima et al. (Lima et al., 2004) on Fleet Size and Mix Vehicle Routing Problem with Fixed Cost (FSMF). However, the vehicle type information is always ignored in these methods (Liu and Lu, 2013). In our study, a new constructive routing algorithm is proposed incorporating the vehicle type information.

2. Ochi and Proposed Constructive Routing Algorithms

An undirected graph is defined by $G = (V, A)$ where V $=$ $\left\{ 0,1,2,...,n\right\}$ V $=$ $\left\{ 0,1,2,...,n\right\}$ is a set composed of $(n + 1)$ vertices, and $A = \{(i, j): i, j \in V, i \neq j\}$ is the set of arcs. The vertex $\frac{0}{0}$ denotes the depot, where the vehicle fleet is initially located, while the set $V' = V - \{0\}$ is composed of the remaining vertices that represent n customers.

It is assumed that each customer $i \in V'$ has a positive demand q_i and depot's demand is always zero. $C = [c_{ii}]$ is the distance matrix where the parameter c_{ii} represents a positive cost or distance between vertices i and j. A heterogeneous fleet of vehicles must be used to supply the customers. The vehicle fleet is composed by a set $\Psi(k) \in \{1,2,...,t\}$ of different vehicle types where t is the number of vehicle types associated with the route, and it is assumed that each vehicle type is available at unlimited numbers. For each vehicle type $i \in \Psi$, Q_i is the capacity, f_i is the fixed cost to be paid, and D_i is the amount of demand collected from or loaded to the vehicle. It is assumed that the fixed costs are increasing with the capacity i.e. $Q_1 < Q_2 < \cdots < Q_t$ and $f_1 < f_2 < \cdots < f_t$ (Ochi et al., 1998; Lima et al., 2004; Baldacci et al., 2008; Subramanian et al., 2012). A route for vehicle type k is defined by the pair $(R, \Psi(k))$ where $R = (i_1, i_2, ..., i_{|R|})$, with $i_1 = i_{|R|} = 0$ and $\{i_2, i_3, ..., i_{|R|-1}\}\subseteq V$, is a simple circuit in G containing the depot. Here, R will be used to refer both to visiting sequence and to the set of customers (including depot) of the route. A route $(R, \Psi(k))$ is feasible if the total demand of the customers visited by the route does not exceed the vehicle capacity Q_k , that is, $\sum_{h=2}^{|R|-1} q_{i_h} \leq Q_k$. The cost of a route corresponds to the sum of the costs of the edges forming the route, plus the fixed cost of the associated vehicle, that is, $\int_{h=1}^{|R|-1} c_{i_h,i_{h+1}}^k + f_k$ (Baldacci et al., 2008).

The route configuration proposed by (Ochi et al., 1998) is achieved by selecting the minimum from the alternatives obtained by the constraint $(Q_k - D_k) *$ f_k . However, our study is based on $(Q_k - D_k)$ constraint for route configuration and then selecting the minimum from the alternatives obtained. The constraints of the related routing strategies are given in Table 1.

Table 1: Proposed Approach and Ochi Approach routing constraint for HFVRP

Routing	Ochi(1998)	Karagul
Construction	$min(Q_k - D_k) * f_k$	$min(Q_k - D_k)$
/ Selection		

In this study, the routing approach in (Ochi et al., 1998) is denoted as Ochi **Minumum Distance Minimum Vertex Algorithm** (**Ochi MinDis-MinVer Algorithm**) and the proposed routing approach is denoted as **Karagul Minumum Distance Minimum Vertex Algorithm** (**Karagul MinDis-MinVer Algorithm**). The Ochi MinDis-MinVer algorithm is demonstrated in Figure 1. The constraint $(Q_k - D_k)$ * f_k is defined with (Residuals*FixedCost). The first obtained path is used for equal minimum (Residuals*FixedCost) of any two paths.

```
start with the Initial Solution Space 
(TSP_order)
for each TSP order
  while {end of the TSP order}
      while {end of the number of 
vehicle_type}
         Construct temporary routings for 
each vehicle_type 
      end {of while}
         Find the 
minimum(Residuals*FixedCost) that is the 
temporary Path
         Assign the vertex and vehicle 
type to the Path
       Calculate Routing Cost, TSP order,
vehicle_type
    end {of while}
      TSP order solution: [Total_Cost 
Routings Type of Vehicles TSP order]
 end {of for} 
Solution Space:[TSP_order solution 
[Total_Cost Routings Type_of_Vehicles 
TSP_order] ]
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Figure 1 : Ochi Minimum Distance Minimum Vertex Algorithm (Ochi MinDis-MinVer Algorithm)

Karagul MinDis-MinVer algorithm is given in Figure 2. For this algorithm, the constraint $(Q_k - D_k)$ is defined with (Residuals). Similar to Ochi MinDis-MinVer Algorithm, for equal minimum (Residuals) of any two paths, the first obtained path is used.

Figure 2 : Karagul Minimum Distance Minimum Vertex Algorithm (Karagul MinDis-MinVer Algorithm)

3. Sample Problem and Solution Phases

An HFVRP problem is defined in order to show the effectiveness of the proposed method in Figure 3. The problem is composed of a depot, two types of vehicles (t1, t2), and 6 customers. The parameters defining the problem are given in Figure 4.

Figure 3 : Representation of the sample problem with vertices and all connections

Figure 4 : Sample problem's distance matrix, customer demands, vehicle types fixed costs and vehicle types capacity

The solution routes of Ochi MinDis-MinVer algorithm for a random TSP order of {2, 3, 4, 5, 6, 7} is shown step by step in Figure 5.

Figure 5 : Ochi Minimum Distance Minimum Vertex Algorithm solution phases for routing TSP order of {2, 3, 4, 5, 6, 7}

The vehicle routes are constructed with respect to $(Q_k - D_k) * f_k$ constraint and vehicles with smaller capacities are considered first. As shown in Figure 5, when customer 2 is considered for t1, the demand is 40 units. As the vehicle capacity will exceed 50, customer 3 cannot be added. Therefore, for vehicle t1 the temporary route is $\{2\}$, the total load quantity is 40 units and residual is 50-40=10 units, and the residual cost is 10*40=400 unit cost.

Similar to t1, when the demands of 40 units from customer 2, 23 units from customer 3 and 15 units from customer 4 are loaded to the vehicle t2 not to exceed 90 unit capacity, 78 unit loading is made in total. The temporary path {2, 3, 4} is obtained. The residual for t2 is 90-78=12 units and the residual cost is 12*70=840 unit cost.

When the residual costs of two vehicles are considered, it is seen that there is 400 units cost for t1 and 840 units cost for t2. Therefore, the first constructed path $R1 = \{\{1-2-1\},\,t1\}$ is taken as it has minimum residual cost. Then, customer {2} is discarded from TSP order.

The un-routed customers {3, 4, 5, 6, 7} are reconstructed for temporary routes. As can be seen from the second phase in Figure 5, firstly for vehicle t1, 23 units from {3}, 15 units from {4} are loaded which in total compose 38 units load. The residual is 12 units and the residual cost is 480 unit cost. Similarly, for vehicle t2, 23 units from {3}, 15 units from {4} and 20 units from {5} are loaded which in total compose 58 unit loads. The residual is 32 units and the residual cost is 2240 units cost. When the residual costs of two vehicles are considered for the second phase, it is seen that there is 480 units cost for t1 and 2240 unit cost for t2. Therefore, the second constructed path $R2 = ({1-3-4-1}, t1)$ is taken as it has minimum residual cost.

Then, customer {3, 4} is discarded from TSP order. The un-routed customers {5, 6, and 7} are reconstructed for temporary routes. As can be seen from the second phase of Figure 5, firstly for vehicle t1, 20 units from {5} is loaded. The residual is 30 units and the residual cost is 1200 unit cost. Similarly, for vehicle $t2$, 60 units from $\{5, 6\}$ are loaded which in total compose 58 unit load. The residual is 30 units and the residual cost is 2100 unit cost. When the residual costs of two vehicles are considered for the second phase, it is seen that there is 1200 unit cost for t1 and 2100 unit cost for t2. Therefore, the third constructed path $R3 = \{1-5-1\}$, t1) is taken as it has minimum residual cost. Then, customer {5} is discarded from TSP order and the unrouted customers {6, 7} are reconstructed for temporary routes.

When the same process is executed for remaining customers {6, 7}, the routes and assigned vehicles are t1 and R4= $({1-6-1}, {t1})$ and R5= $({1-7-1}, {t1})$. Thus, for Ochi MinDis-MinVer algorithm the routing process for the TSP orders is completed. The summary table for the routings and costs are given in Figure 7.

In Figure 6, the solution routes of Karagul MinDis-MinVer algorithm for the same TSP order given in Figure 5 for Ochi MinDis-MinVer algorithm, is shown step by step.

Figure 6 : Karagul Minimum Distance Minimum Vertex Algorithm solution phases for routing TSP order {2, 3, 4, 5, 6, 7}

The vehicle routes are constructed with respect to $(Q_k - D_k)$ constraint and vehicles with smaller capacities are considered first. As shown in Figure 6, when customer {2} is considered for t1, the demand is 40 units. As the vehicle capacity will exceed 50, customer {3} cannot be added. Therefore, for vehicle t1 the temporary route is $\{2\}$, the total load quantity is 40 units and residual is 50-40=10 units.

Similar to t1, when the demands of 40 units from customer {2}, 23 units from customer {3} and 15 units from customer {4} are loaded to the vehicle t2 not to exceed 90 unit capacity, 78 unit loading is made in total. The temporary path {2, 3, 4} is obtained. The residual for t2 is 90-78=12 units. When the residuals of two vehicles are considered, it is seen that there is 10 unit for t1 and 12 unit for t2. Therefore, the first constructed path R1=({1-2-1}, t1) is taken as it has minimum residual. Then, customer {2} is discarded from TSP order.

The un-routed customers {3, 4, 5, 6, 7} are reconstructed for temporary routes. As can be seen from the second phase in Figure 6, firstly for vehicle t1, 23 units from $\{3\}$, 15 units from $\{4\}$ are loaded which in total compose 38 unit load. The residual is 12 units. Similarly, for vehicle t2, 23 units from {3}, 15 units from {4} and 20 units from {5} are loaded which in total compose 58 unit load. The residual is 32 units. When the residual of two vehicles are considered for the second phase, it is seen that there is 12 unit for t1 and 32 unit for t2. Therefore, the second constructed path $R2 = ({1-3-4-1})$, t1) is taken as it has minimum residual. Then, customer {3,4} are discarded from TSP order. The un-routed customers {5, 6, 7} are reconstructed for temporary routes. As can be seen from the second phase in Figure 6, firstly for vehicle t1, 20 units from {5} is loaded. The residual is 30 units. Similarly, for vehicle t2, 60 units from {5,6} are loaded. The residual is 30 units. When the residual of two vehicles are considered for the second phase, it is seen that there is 30 unit for t1 and

30 unit for t2. Therefore, the residuals for both vehicles are equal and as assumed previously the first obtained route is selected. Therefore, the third constructed path $R3 = ({1-5-1}, t1)$ is taken as it has minimum residual. Then, customer {5} is discarded from TSP order and the un-routed customers {6, 7} are reconstructed for temporary routes.

When the same process is executed for remaining customers {6, 7}, the route and assigned vehicle are R4=({1-6-7-1}, t2). Thus, for Karagul MinDis-MinVer algorithm the routing process for the TSP orders is completed. The summary table for the routings and costs are given in Figure 7.

		$\overline{2}$	$\overline{\mathbf{3}}$	$\overline{4}$	5 6	$\overline{7}$
	R Name	Route	т	Fixed Costs	Route Distance	Route Cost
Ochi Routing	R1	$1 - 2 - 1$	t1	40	120	160
	R2	$1 - 3 - 4 - 1$	t1	40	165	205
	R ₃	$1 - 5 - 1$	t1	40	100	140
	R ₄	$1 - 6 - 1$	t1	40	140	180
	R ₅	$1 - 7 - 1$	t1	40	120	160
						845
	R1	$1 - 2 - 1$	t1	40	120	160
Karagul Routing	R ₂	$1 - 3 - 4 - 1$	t1	40	165	205
	R ₃	$1 - 5 - 1$	t1	40	100	140
	R ₄	$1 - 6 - 7 - 1$	t2	70	200	270
						775

Figure 7 : Ochi and Karagul Routings Algorithms solutions results for TSP order {2, 3, 4, 5, 6, 7}

Different routes are obtained by using the given algorithms can be seen from Figure 7. When the total costs of two solutions are compared it is seen that Karagul algorithm is better for the given problem and the TSP order. The graph of routes for both Ochi and Karagul routing algorithms are given in Figure 8.

Figure 8 : Ochi and Karagul Routings Algorithms solutions results for TSP order {2, 3, 4, 5, 6, 7}

Then, Ochi and Karagul routing approaches are compared for the same sample problem with different initial TSP orders. Solutions are obtained based on Ochi and Karagul routing approaches for two random TSP orders that are {3, 4, 2, 6, 5, 7} and {2, 7, 6, 5, 3, 4}. These solutions are given in Figure 9.

Figure 9 : Ochi MinDis-MinVer Algorithm solutions for {3, 4, 2, 6, 5, 7} TSP order

As can be seen from Figure 9, the constructed routes and the types of vehicles assigned to each route with Ochi MinDis-MinVer Algorithm are R1=({1-3-4-1}, t1), $R2 = \{1-2-1\}$, t1), $R3 = \{\{1-6-1\}$, t1), $R4 = \{\{1-5-1\}$, t1), $R5 = ({1-7-1}, t1)$, respectively.

Figure 10 : Karagul MinDis-MinVer Algorithm solutions for {3, 4, 2, 6, 5, 7} TSP order

As can be seen from Figure 10, the constructed routes and the types of vehicles assigned to each route with Karagul MinDis-MinVer Algorithm are R1={1-3-4-1}, t1), R2=({1-2-1}, t1), R3=({1-6-1}, t1), R4=({1-5-7-1}, t2), respectively. The solutions and costs obtained from the algorithms are shown in Figure 11.

		$\overline{\mathbf{3}}$	$\overline{4}$	$\overline{2}$	6	5	$\overline{7}$
	R Name	Route	т	Fixed Costs		Route Distance	Route Cost
Ochi Routing	R1	$1 - 3 - 4 - 1$	t1	40	165		205
	R ₂	$1 - 2 - 1$	t1	40	120		160
	R ₃	$1 - 6 - 1$	t1	40	140		180
	R ₄	$1 - 5 - 1$	t1	40	100		140
	R ₅	$1 - 7 - 1$	t1	40		120	160
							845
	R1	$1 - 3 - 4 - 1$	t1	40		165	205
	R2	$1 - 2 - 1$	t1	40		120	160
Karagul Routing	R ₃	$1 - 6 - 1$	t1	40		140	180
	R ₄	$1 - 5 - 7 - 1$	t2	70		200	270
							815

Figure 11 : Ochi and Karagul Routings Algorithms solutions results for {3, 4, 2, 6, 5, 7} TSP order

The number of routes constructed with Karagul MinDis-MinVer Algorithm is less than Ochi MinDis-MinVer Algorithm. Also total costs are 815 and 845 monetary-units for Karagul and Ochi MinDis-MinVer Algorithms, respectively. The graph representations of constructed routes of both algorithms are given in Figure 12.

Figure 12 : Ochi and Karagul Routings Algorithms solutions graphs for {3, 4, 2, 6, 5, 7} TSP order

Figure 13 : Ochi MinDis-MinVer Algorithm solutions for {2, 7, 6, 5, 3, 4} TSP order

As can be seen from Figure 13, the constructed routes and the types of vehicles assigned to each route with Ochi MinDis-MinVer Algorithm are R1=({1-2-1}, t1), $R2 = ({1-7-1}, t1), R3 = ({1-6-1}, t1), R4 = ({1-5-3-1}, t1),$ $R5=(1-4-1), t1$, respectively.

Figure 14 : Karagul MinDis-MinVer Algorithm solutions for {2, 7, 6, 5, 3, 4} TSP order

As can be seen from Figure 14, the constructed routes and the types of vehicles assigned to each route with Karagul MinDis-MinVer Algorithm are R1=({1-2-7-1}, t2), $R2 = ({1-6-5-3-1}, t2)$, and $R3 = ({1-4-1}, t1)$, respectively.

Figure 15 : Ochi and Karagul Routings Algorithms solutions results for {2, 7, 6, 5, 3, 4} TSP order

When Figure 15 is reviewed, it is seen that while R1, R2, R3, R4 and R5 routes are obtained with a total cost of 843 money unit from Ochi MinDis-MinVer Algorithm, R1, R2, R3 routes are obtained with a total cost of 787 monetary-units from Karagul MinDis-MinVer Algorithm.

Both the number of routes and total cost are less for Karagul approach than Ochi approach. The graph representations of constructed routes for both methods are given in Figure 16.

Figure 16 : Ochi and Karagul Routings Algorithms solutions graphs for {2, 7, 6, 5, 3, 4} TSP order

From the sample routing problem, the difference between the proposed method and the current solutions are analyzed. In the next section, Golden's test instances are used to see the performance of the proposed method on some known test problems from the literature.

4. Computational Results

The proposed method is tested by using 12 sample problems obtained from Golden et al. (Golden et. al., 1984) and extensively used in the literature for FSMF. The calculations are constructed from two phases: the first step is obtaining the initial solution space, and the second step is the route configuration and the selection of the appropriate constraint. The initial solution space is generated based on the method presented by Liu et al. (Liu et al., 2009) where the initial solution space is composed of 3 parts: the first part from the Savings Algorithm, the second part from the Sweep Algorithms and the rest of the individuals are generated randomly. In our study, on the other hand, the randomly generated individuals are not used. The solutions of the Savings and Sweep algorithms are obtained by using "Matlog: Matlab Logistic Engineering Toolbox" (Kay, 2013).

The problems are tested on a computer with Pentium Core Duo i7 processor and 4 GB RAM.

The results obtained on the basis of the initial solutions from Sweep and Savings algorithms are listed in Table 2 where P.No is the problem number as given by Golden et al. (Golden et al., 1984), BKS is the best known solution in the literature, Solution is the Karagul and Ochi solutions obtained for the given problems with this study, Deviation is the percent deviation from the best known solution, Time is the solution time in seconds and S.S. is the dimension of the initial solution space. The initial solutions are obtained excluding the depot in the form of TSP order. Then the routes are configured with respect to the related methods. From the alternative route solutions, the type of vehicle that provides the minimum condition is selected as the optimal route. The periods for obtaining the initial solutions are not considered for the solution times in Table 2. Therefore, the solution times are solely giving the execution times of the algorithms.

When Table 2 is reviewed; for 7 of 12 test problems Karagul MinDis-MinVer Algorithm has better total cost values. Also, for 3 problems it has same total costs with Ochi MinDis-MinVer Algorithm. With Ochi MinDis-MinVer Algorithm, only 2 of 12 test problems have best total cost values. When the average performances are compared, the proposed method has better characteristics from time complexity and total cost point of view. Based on the given tests, Karagul MinDis-MinVer Algorithm can be proposed as a new constructive routing algorithm for HFVRP.

5. Conclusions and Discussion

In this study, a new constructive route configuration different from the method recommended by Ochi et al and an approach certainly competitive with their method are proposed. The problems in the literature are solved using a seeding with Sweep and Savings algorithms proposed by Liu-Huang-Ma (Liu et al., 2009). When the proposed method is logically compared for different situations, it gives better results than the approach of Ochi et al (Ochi et al., 1998). Thus, the new method can be suggested both for route configuration and route selection in heterogeneous VRPs. The solution given in this study can be enriched using different initial solution generation methods and new hybrid solution methods can be obtained by combining with heuristic search methods.

Acknowledgements

The authors are grateful to reviewers for valuable contributions. The author gratefully acknowledges that research for this paper is financially supported by the Pamukkale University Scientific Research Projects Unit with grant no. 2013-BSP026.

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